CONTRIBUTION FROM THE INSTITUT FÜR PHYSIKALISCHE CHEMIE DER UNIVERSITÄT ERLANGEN-NÜRNBERG, 8520 ERLANCEN, GERMANY

# The Mechanism of Formation of Binuclear Isopolybases

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### *Received November 14,1968*

In connection with studies concerning the kinetics ol the reactions that lead to isopolybases, there arises the question whether a reaction of the type

$$
mM^{z+} + nH_2O \implies M_m(OH)_n^{(z-n)+} + nH^+
$$
 (1)

may have something in common with the simple complex-forming reaction, type 2, of the same metal  $M^{z+} + X^{y-} \implies MX^{(z-y)+}$  *(2)* 

$$
\mathbf{M}^{z+} + \mathbf{X}^{y-} \longrightarrow \mathbf{M} \mathbf{X}^{(z-y)+} \tag{2}
$$

cation  $M^{z+}$ . As will be shown in two cases where sufficient kinetic data exist, namely, with the formation of the binuclear iron(III)-hydroxo complex  $(FeOH)<sub>2</sub><sup>4+</sup>$ and with the formation of the binuclear vanadylhydroxo complex  $(OVOH)_2^2$ <sup>+</sup>, a simple relation between the reaction of type 1 and reactions of type *2* exists: for both reactions the spontaneous exchange of water molecules in the inner hydration sphere of the monohydroxo complex of the participating metal cations obviously is the rate-determining step.

As has been shown previously<sup>1</sup> the formation of the binuclear iron(III) complex (FeOH)<sub>2</sub><sup>4+</sup> proceeds *via* the bimolecular reaction of two iron(II1)-nionohydroxo ions

$$
2\mathrm{FeOH^{2+}}\xrightarrow[k_{11}]{k_{12}}(\mathrm{FeOH})_{2}^{4+}\tag{3}
$$

with the bimolecular rate constant  $k_{12} = 450$   $M^{-1}$  sec<sup>-1</sup>  $(\text{at } \mu = 0.6 \text{ } M \text{ and at } 25^{\circ}).$ 

If the Eigen mechanism for the formation of complexes in solution is applied to reaction **3,** then the following three-step reaction scheme for reaction **3** can be postulated

be postulated  
\n
$$
2FeOH(H_2O)_s^2 + \frac{K_0}{\text{fast}} (FeOH(H_2O)_b)_2^4 + \frac{k_{33}}{k_{32}}
$$
\nI II\n
$$
(H_2O)_bFe-O-Fe(H_2O)_4^{4+} + H_2O
$$
\n
$$
HOH
$$
\nIII\n(4)  
\n
$$
(H_2O)_bFe-O-Fe(H_2O)_4^{4+} + \frac{O}{\text{fast}} (H_2O)_4Fe
$$
\n
$$
HOH
$$
\n
$$
HOH
$$
\n
$$
H_2O
$$
\n
$$
H_2O
$$

(a) The equilibrium  $I \rightleftarrows II$  (with nearly diffusioncontrolled rates) is rapidly established between free (1) H. Wendt, *Z. Elehtvochem.,* **66,** 235 (1962).

iron(lI1)-monohydroxo cations and two iron(lI1) monohydroxo cations with still intact inner hydration spheres touching each other in close contact. Equilibrium  $I \rightleftharpoons II$  is characterized by the formation constant  $K_0$  for the "contact complex."

The contact complex.<br>
(b) The rate-determining step  $II \rightleftarrows III$  is the loss of one water molecule from the inner hydration sphere of one of the two cations that form the "contact complex." It is to be postulated that the loss of this water molecule is immediately followed by the insertion of a hydroxyl ion that is bound to the neighboring iron-hydroxo cation, so that one OH bond between both cations of the "contact complex" is formed.

Then follows the fast formation of the second (c) OH bond by loss of another water molecule and insertion of a second hydroxyl ion (III  $\rightleftharpoons$  IV). (This reaction might be a fast innerniolecular protolytic reaction that leads to a  $\mu$ -oxo complex instead of a diol complex as well

$$
\begin{array}{c} (H_2O)_bFe-O-Fe(H_2O)_4{}^{4+}\Longleftrightarrow (H_2O)_bFe-O-Fe(H_2O)_5{}^{4+}\\ \text{H~OH} \end{array}
$$

The question whether the dinuclear iron (III) complex is a diol or a  $\mu$ -oxo complex is not yet settled.)

Then from eq 3 and 4, with the stability constant  $K_0$ being small, the measured bimolecular rate constant *klz*  can be expressed

$$
k_{12} = k_{23} K_0 \tag{5}
$$

*kzs* is the monomolecular rate constant for the transformation of the "contact complex" into the binuclear isopolybase.  $K_0$  can be estimated according to Fuoss.<sup>2</sup>

If we insert in Fuoss' formula the macroscopic dielectric constant of water  $\epsilon = 80$  and a distance between the centers of the cations in the "contact complex" of *d* = 5 Å we get  $K_0(2+,2+)_{\mu=0} = 1.2 \times 10^{-3} M^{-1}$  (25°,  $d= 5$  Å). The rate constant  $k_{12}$  can be extrapolated to zero ionic strength by use of the Bjerrum theory and the Davies formula:<sup>3</sup>  $k_{12}(\mu = 0) = 25$   $M^{-1}$  sec<sup>-1</sup>. Then we get from eq  $5 k_{23} = 2.2 \times 10^4 \text{ sec}^{-1}$ .

From the kinetic investigation of the hydroxyl ion catalyzed path of the complex formation of the iron- (111) cation the rate of water exchange in the inner hydration shell of the iron-monohydroxo ion can be estimated<sup>4-6</sup> as  $k_{\text{H}_2O\text{ exch}}(\text{FeOH}^{2+}) \approx 5 \times 10^3 \text{ sec}^{-1}$  $(25^{\circ})$ . Now as  $k_{23}$  and  $k_{H_2O}$  exch are of the same order of magnitude, one may conclude that for the formation of the binuclear isopolybase the rate-determining step is the spontaneous water exchange in the inner hydration sphere of the monomer  $FeOH<sup>2+</sup>$ . (The contact distance of 5 Å used to determine  $K_0$  previously is somewhat arbitary and has no definite physical meaning.

<sup>(2)</sup> R. M. Fuoss, *J. Am.* Chem. *Soc.,* **80,** 5059 (1958). **(8)** C. W. Davies, "Ion Association," Butterwortb and Co. Ltd., London,

<sup>1962.</sup> 

**<sup>(4)</sup>** D. Seewald and N. Sutin, *Inovg.* Chem., *2,* 643 (1963).

*<sup>(5)</sup>* H. Wendt and H. Strehlow, *Z. Elektvochem.,* **66,** 223 (1962).

<sup>(6)</sup> H. Wendt, Habilitationsarbeit, Erlangen, 1967; to be submitted for publication.

It has been chosen as this value together with  $\epsilon = 80$ gives the best fit between calculated and experimentally determined stability constants for outer-sphere complexes<sup>7</sup> of  $Cr^{3+}$  and  $Co^{3+8}$  as well as for the complex  $OVH<sub>2</sub>OSO<sub>4</sub>$ .)

The same seems to hold for the hydrolysis reaction of the vanadyl cation. This reaction according to Rossotti and Rossotti<sup>9</sup> leads to the formation of a binuclear isopolybase

$$
2VO^{2+} + 2H_2O \xrightarrow{\sim} (VOOH)_2^{2+} + 2H^+ \tag{6}
$$

It is possible to study this reaction with the stoppedflow method.<sup>10</sup>

A rate law is found which formally allows for the bimolecular combination of two vanadyl-monohydroxo cations to the dimer

$$
\text{limer} \quad\n \begin{aligned}\n &2\text{VOOH} + \frac{k_{12}}{k_{21}} \left(\text{OVOH}\right)_2{}^{2+}\n \end{aligned}\n \tag{7}
$$

with  $k_{12} = 2 \times 10^4 M^{-1} \text{ sec}^{-1} (\text{at } \mu = 0.3 M \text{ and at } 25^\circ)$ and  $k_{21} = 20$  sec<sup>-1</sup>. Then by extrapolation to zero ionic strength we get  $k_{12} (\mu = 0) = 8 \times 10^3 M^{-1} \text{ sec}^{-1}$ . Applying eq 5 and taking from the formula of Fuoss, $2$  $K_0(+1,+1) = 8 \times 10^{-2} M^{-1} (25^\circ, d = 5 \text{ Å}).$  We finally get  $k_{23} = 10^5$  sec<sup>-1</sup>.

Again from the hydroxyl ion catalyzed path of the complex-forming reactions of the vanadyl ion<sup>8,11</sup> the exchange rate of water in the inner hydration sphere of the vanadyl-monohydroxo cation can be estimated as  $k_{\text{H}_2O\text{ exch}}(\text{OVOH}^+) = 3 \times 10^4 \text{ sec}^{-1}$ . Since in this case, too, the rate constant for the spontaneous water exchange and *kz3* are of the same order of magnitude, we may conclude that also with the formation of the binuclear complex  $(OVOH)<sub>2</sub><sup>2+</sup>$  the rate-determining step is the water exchange in the inner hydration sphere of the monomeric species  $OVOH(H<sub>2</sub>O)<sub>4</sub> +$ .

It should be pointed out, however, that into the value of *ka3* enter all possible oversimplifications or mistakes of the Fuoss model. It is possible to apply the Fuoss model to all combinations of interacting species including equally or oppositely charged ions and ion dipoles since in this model only coulombic interaction and the volume of the complex-forming species are considered. However, there always arises the question of the appropriate "contact distance." The "contact distance" of two tightly solvated cations could well be somewhat greater than for solvated cation-anion complexes. Inserting 6 Å instead of 5 Å increases  $K_0(2+,2+)$  and decreases  $k_{23}$ (Fe<sup>3+</sup>) by a factor of 5 and  $K_0(1+,1+)$ and  $k_{23}(VO^{2+})$  by a factor of 2, respectively. This gives a better fit of  $k_{23}$  and  $k_{H_2O\text{ exch}}$  in both cases. However, although the values of  $K_0$  used above may thus be very approximate, it is quite clear that  $k_{23}$  and  $k_{\text{H}_2O\text{ exch}}$  at any rate are of the same order of magnitude.

Obviously the formation also of other binuclear

hydroxo complexes and certain inner-sphere redox reactions are expected to proceed *via* the same simple mechanism, which has long been known to operate in a general way with the complex-forming reactions of solvated cations and no special type of mechanism must be postulated for the olation reactions, which lead to binuclear isopolybases. So the suggestion of Eigen and Wilkins<sup>12</sup> can be confirmed although they used in their paper as a proof of their idea the direct comparison of bimolecular  $(k_{12}$  for the iron reaction) and monomolecular rate constants  $(k_{\text{H}_2O}$  exch for FeOH<sup>2+</sup> which was obviously wrong) which can only be compared directly, when  $K_0$  is approximately 1  $M^{-1}$ .

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## Association of  $Cd^{2+}$  and Br<sup>-</sup> in the Solvent  $KNO_3 + Ca(NO_3)_2 + H_2O^{1a}$

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#### *Received December 16, 1968*

The solution chemistry of electrolytes at concentrations intermediate between anhydrous fused salts and "ordinary" aqueous electrolytes has received little attention, in spite of its importance in the development of theories of electrolyte solutions.<sup>2</sup> The temperature dependence and water concentration dependence of equilibrium constants for the association<br>  $Cd^{2+} + Br^- \implies CdBr^+$  (1)

$$
Cd^{2+} + Br^- \rightleftharpoons CdBr^+ \tag{1}
$$

in the solvent {equimolar  $(Li,K)NO<sub>3</sub>$ } + H<sub>2</sub>O containing up to 50 mol  $\%$  water have supported a quasilattice model of competing association and hydration equilibria.<sup>3</sup>

The present work is part of an extension of these studies to other solvent systems. Studies of transport properties<sup>4,5</sup> and volumetric properties<sup>6</sup> in  $Ca(NO<sub>3</sub>)<sub>2</sub>$ .  $4H<sub>2</sub>O$  and in its mixtures with  $KNO<sub>3</sub>$  have suggested that these hydrate melts may be considered as analogs of molten salts, consisting of nitrate ions and hydrated cations. In this note me describe measurements of the

<sup>(7)</sup> F. Basolo and R. G. Pearson, "Mechanism of Inorganic Reactions," John Wiley &Sons, Inc., New York, N. *Y.,* 1960, **p** 380.

<sup>(8)</sup> H. Strehlow and H. Wendt, *Inorg. Chem.*, 2, 6 (1963).

<sup>(9)</sup> F. Rossotti and H. *S.* Iiossotti, *Ada Chum. Sca?zd.,* **9,** 1177 (1955). (10) B. Lutz and H. Wendt, to be submitted for publication.

<sup>(11)</sup> **A.** Schlund and H. Wendt, *Bey. Buizseizges. Physik. Cheiiz.,* **72,** 652 (1968).

**<sup>(12)</sup>** M. Eigen and R. G. Wilkins in "Mechanisms of Inorganic Reactions," Advances in Chemistry Series, No. 49, American Chemical Society, Washington, **1).** C., 1965, **p** *55.* 

**<sup>(1)</sup>** (a) Research sponsored **by** the U. *S.* Atomic Energy Commission under contracts with the Union Carbide Corp. and with the University of Maine. (h) Oak Ridge National Laboratory. (c) National Science Foundation Cooperative Fellow at the University of Maine, 1964-1966.

**<sup>(2)</sup>** J. Braunstein, *Inoug. Chim. Acta Rev.,* **2,** 19 (1968). **(3)** (a) J. Braunstein, *J. Phys. Chem.,* **71,** 3402 (1967); (b) P. C. Lam-

mers and J. Braunstein *ibid.,* **71,** 2636 (1967).

<sup>(4)</sup> C. T. Moynihan, *ibid.,* **70,** 3399 (1966).

<sup>(5)</sup> J. Braunstein, L. Orr, A. R. Alvarez-Funes, and H. Braunstein, *J. Eleclionnal. Chem.,* **15,** 337 (1967).

<sup>(6)</sup> J. Braunstein, L. Orr, and TV, Macllonald, *J. Chem. Eizg. Data,* **l?,**  415 (1967).